



2. Let non-collinear unit vectors \hat{a} and \hat{b} form an acute angle. A point P moves so that at any time t the position vector \overrightarrow{OP} (where O is the origin) is given by $\hat{a} \cosh + \hat{b} \sin t$. When P is farthest from origin O, let M be the length of \overrightarrow{OP} and \hat{u} be the unit vector along \overrightarrow{OP} . Then,

(A)
$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$$
 and $M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}}$
(B) $\hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|}$ and $M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}}$
(C) $\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$ and $M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}}$
(C) $\hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|}$ and $M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}}$

Sol. (A)

 \hat{u} is along internal angle bisector of $\hat{a} \& \hat{b}$

$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|}$$

$$\stackrel{\rightarrow}{OP} = \hat{a}\cos t + \hat{b}\sin t$$

$$\stackrel{\rightarrow}{|OP|^2} = 1 + 2\hat{a} \cdot \hat{b}\sin 2t$$

$$= 1 + \hat{a} \cdot \hat{b}\sin 2t$$

$$M^2 = 1 + \hat{a} \cdot \hat{b}$$

$$M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}}$$

3. Let $I = \int \frac{e^{x}}{e^{4x} + e^{2x} + 1} dx$, $J = \int \frac{e^{-x}}{e^{-4x} + e^{-2x} + 1} dx$. The, for an arbitrary constant C, the value of J - I equals (A) $\frac{1}{2} log \left(\frac{e^{4x} - e^{2x} + 1}{e^{4x} + e^{2x} + 1} \right) + C$ (B) $\frac{1}{2} log \left(\frac{e^{2x} + e^{x} + 1}{e^{2x} - e^{x} + 1} \right) + C$ (C) $\frac{1}{2} log \left(\frac{e^{2x} - e^{x} + 1}{e^{2x} - e^{x} + 1} \right) + C$ (C) $\frac{1}{2} log \left(\frac{e^{2x} - e^{x} + 1}{e^{2x} - e^{x} + 1} \right) + C$ (C) $\frac{1}{2} log \left(\frac{e^{4x} + e^{2x} + 1}{e^{4x} - e^{2x} + 1} \right) + C$ (C) $\frac{1}{2} log \left(\frac{e^{4x} - e^{2x} + 1}{e^{4x} - e^{2x} + 1} \right) + C$ (C) $\frac{1}{2} log \left(\frac{e^{-x}}{e^{4x} - e^{2x} + 1} \right) + C$



$$\begin{aligned} \Rightarrow J - I &= \int \left(\frac{e^{3x} - e^x}{e^{4x} + e^{2x} + 1} \right) dx \\ \Rightarrow J - I &= \int \frac{e^{2x}(e^x - e^{-x})}{(e^{4x} + e^{2x} + 1)} dx \\ J - I &= \int \frac{(e^x - e^{-x})}{e^{2x} + 1 + e^{-2x}} dx \end{aligned}$$

$$Put e^x = t \Rightarrow dx = \frac{dt}{e^x} \text{ or } \frac{dt}{t} \\ \Rightarrow J - I &= \int \frac{(t - 1/t)}{(t^2 + 1 + 1/t)} \frac{dt}{t} \\ &= \int \frac{\left(1 - \frac{1}{t^2}\right)}{\left(t^2 + \frac{1}{t^2} + 1\right)} dt \\ J - I &= \int \frac{\left(1 - \frac{1}{t^2}\right)}{\left(t + \frac{1}{t}\right)^2 - 1} dt \\ Put t + \frac{1}{t} &= u \Rightarrow \left(1 - \frac{1}{t^2}\right) dt = du \\ \Rightarrow J - I &= \int \frac{du}{u^2 - 1} \\ \Rightarrow J - I &= \int \frac{du}{u^2 - 1} \\ \Rightarrow J - I &= \frac{1}{2} \int \frac{du}{u - 1} - \frac{1}{2} \int \frac{du}{u + 1} \\ \therefore J - I &= \frac{1}{2} \log \frac{u - 1}{u + 1} \\ \therefore J - I &= \frac{1}{2} \log \frac{u - 1}{u + 1} \end{aligned}$$

$$as u = t + \frac{1}{t}$$



$$\therefore \quad J-I = \frac{1}{2} \log \left(\frac{t^2 - t + 1}{t^2 + t + 1} \right)$$

$$\therefore \quad J-I = \frac{1}{2} \log \left(\frac{e^{2x} - e^x + 1}{e^{2x} + e^x + 1} \right) \qquad \text{as } t = e^x$$

4. Consider three points. $P = (-\sin(\beta - \alpha), -\cos\beta), Q = (\cos(\beta - \alpha), \sin\beta)$ and

 $\mathsf{R} = (\cos(\beta - \alpha + \theta), \sin(\beta - \theta)), \text{ where } 0 < \alpha, \beta, \theta < \frac{\pi}{4}. \text{ Then,}$

(A) P lies on the line segment RQ

(C) R lies on the line segment $\ensuremath{\mathsf{QP}}$

Sol. (D) Let $\alpha = \beta = \theta = \pi/6$

$$\therefore \mathsf{P} = \left(\mathsf{O}; -\frac{\sqrt{3}}{2}\right), \mathsf{Q} = \left(\mathsf{1}, \frac{1}{2}\right) \sqrt{\mathsf{R}} = \left(\frac{\sqrt{3}}{2}, \mathsf{O}\right)$$

which are non-collinear therefore option (D) is correct

5. An experiment has 10 equally likely outcomes. Let A and B be two non-empty events of the experiment. If A consists of 4 outcomes, the number of outcomes that B must have so that A and B are independent, is

(A) 2, 4 or 8 (B) 3, 6 or 9

(c) 4 or 8

(B) Q lies on the line segment PR

(D) P,Q,R are non-collinear

(d) 5 or 10

Sol. (D) By using option (D)

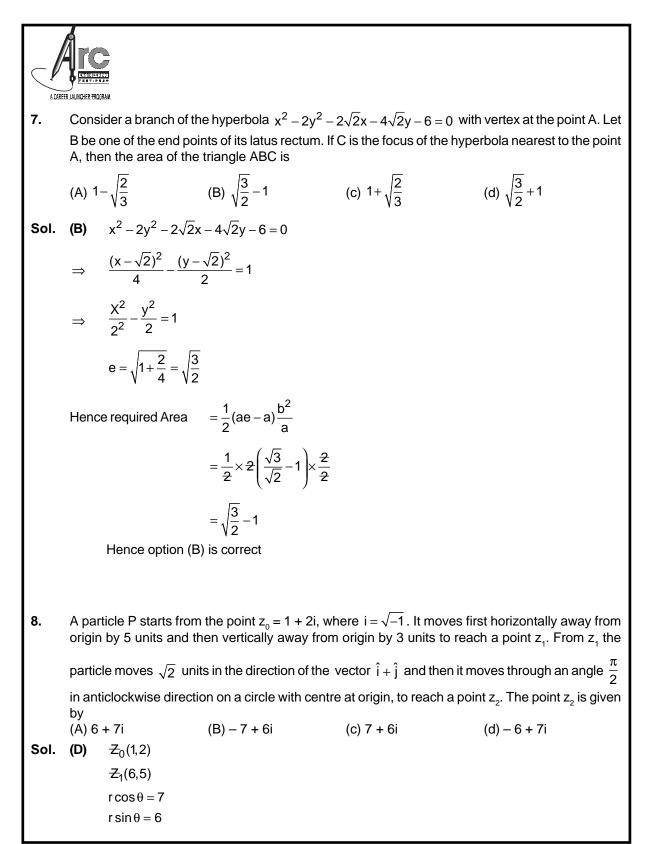
$$P(A \cap B) = \frac{4}{10} \times \frac{5}{10} = \frac{2}{10}$$

$$P(A \cap B) = \frac{4}{10} \times \frac{10}{10} = \frac{4}{10}$$

hence option (D) is correct

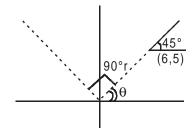


6. The area of the region between the curves
$$y = \sqrt{\frac{1+\sin x}{\cos x}}$$
 and $y = \sqrt{\frac{1-\sin x}{\cos x}}$ bounded by the lines
 $x = 0$ and $x = \frac{\pi}{4}$ is
(A) $\int_{0}^{\sqrt{2}-1} \frac{1}{(1+t^{2})\sqrt{1-t^{2}}} dt$ (B) $\int_{0}^{\sqrt{2}-1} \frac{4t}{(1+t^{2})\sqrt{1-t^{2}}} dt$
(C) $\int_{0}^{\sqrt{2}+1} \frac{4t}{(1+t^{2})\sqrt{1-t^{2}}} dt$ (D) $\int_{0}^{\sqrt{2}+1} \frac{1}{(1+t^{2})\sqrt{1-t^{2}}} dt$
Sol. (B)
Desired Area $= \int_{0}^{\pi/4} \left(\sqrt{\frac{1+\sin x}{\cos x}} - \sqrt{\frac{1-\sin x}{\cos x}} \right) dx$
 $= \int_{0}^{\pi/4} \left(\sqrt{\frac{1+\frac{2\tan x/2}{1+\tan^{2} x/2}}{1-\tan^{2} x/2}} - \sqrt{\frac{1-\frac{2\tan x/2}{1+\tan^{2} x/2}}{1+\tan^{2} x/2}} \right) dx$
 $= \int_{0}^{\pi/4} \left(\frac{|(\tan x/2+1)|}{\sqrt{1-\tan^{2} x/2}} - \frac{|(1-\tan x/2)|}{\sqrt{1-\tan^{2} x/2}} \right) dx$
 $= \int_{0}^{\pi/4} \frac{2\tan x/2}{\sqrt{1-\tan^{2} x/2}} dx$ [as $0 < x < \pi/4$]
put $\tan x/2 = t$
 $dx = \frac{2dt}{\sqrt{1-t^{2}}} \cdot \frac{2dt}{(1+t^{2})}$
Area $= \sqrt{\frac{\sqrt{2}-1}{0} \frac{2t}{\sqrt{1-t^{2}}} \cdot \frac{2dt}{(1+t^{2})}$





 $\Xi_2(r\cos(\theta+90^\circ), r\sin(\theta+90^\circ))$



= $\frac{1}{2}$ $(r\cos(\theta + 90^\circ), r\sin(\theta + 90^\circ))$

 $\Rightarrow = \frac{1}{2}(-r\sin\theta, r\cos\theta)$

$$\therefore \quad \frac{1}{2} = -6 + 7i$$

9. Let the function
$$g: (-\infty,\infty) \to \left(-\frac{\pi}{2},\frac{\pi}{2}\right)$$
 be given by $g(u) = 2\tan^{-1}(e^u) - \frac{\pi}{2}$. Then, g is

(A) even and is strictly increasing in $(0,\infty)$

(B) odd and is strictly decreasing in $(-\infty,\infty)$

- (C) odd and is strictly increasing in $(-\infty,\infty)$
- (D) neither even nor odd, but is strictly increasing in $(-\infty,\infty)$

Sol. (C)

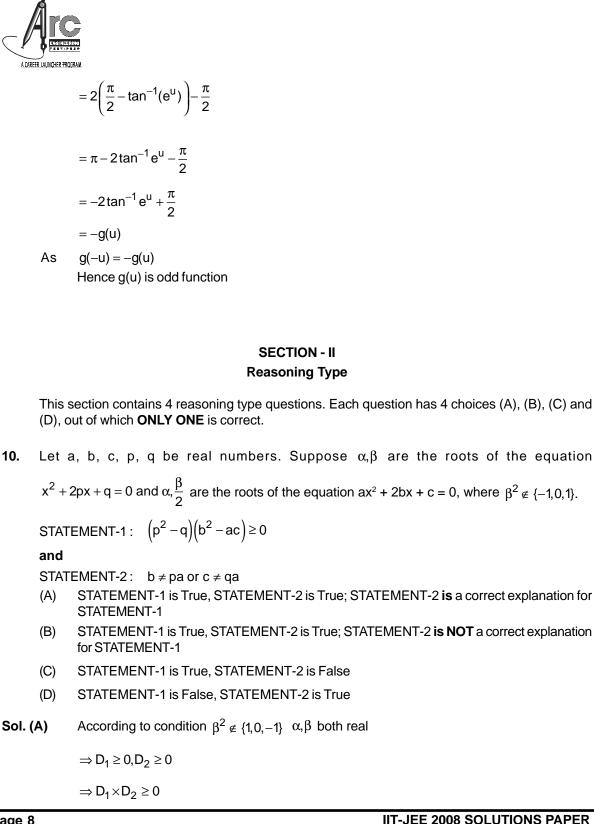
g(u) = 2 tan⁻¹(e^u) -
$$\frac{\pi}{2}$$

∴ g(u) = 2 $\frac{1}{(1+e^{2u})}e^{1}$

Hence, monotonically increasing in $(-\infty,\infty)$

Now
$$g(-u) = 2\tan^{-1}(e^{(-u)}) - \frac{\pi}{2}$$

= $2\tan^{-1}\left(\frac{1}{e^{u}}\right) - \frac{\pi}{2}$
= $2\cot^{-1}(e^{u}) - \frac{\pi}{2}$





& b ≠ pa,c ≠ qa

11. Consider

 $L_1: 2x + 3y + p - 3 = 0$

 $L_2: 2x + 3y + p + 3 = 0$

where p is a real number, and $C: x^2 + y^2 + 6x - 10y + 30 = 0$.

STATEMENT-1: In line L_1 is a chord of circle C, then line L_2 is not always a diameter of circle C.

and

STATEMENT-2: In line L_1 is a diameter of circle C, then line L_2 is not a chord of circle C.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
- (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
- (C) STATEMENT-1 is True, STATEMENT-2 is False
- (D) STATEMENT-1 is False, STATEMENT-2 is True
- Sol. (C) If L₁ is the diameter then p = -6L₂ becomes 2x + 3y - 3 = 0Now distance of (-3, 5) From L₂ is

$$\left|\frac{-6+15-3}{\sqrt{13}}\right| = \frac{6}{\sqrt{13}} < 2$$

$$\Rightarrow L_2 \text{ is chord}$$

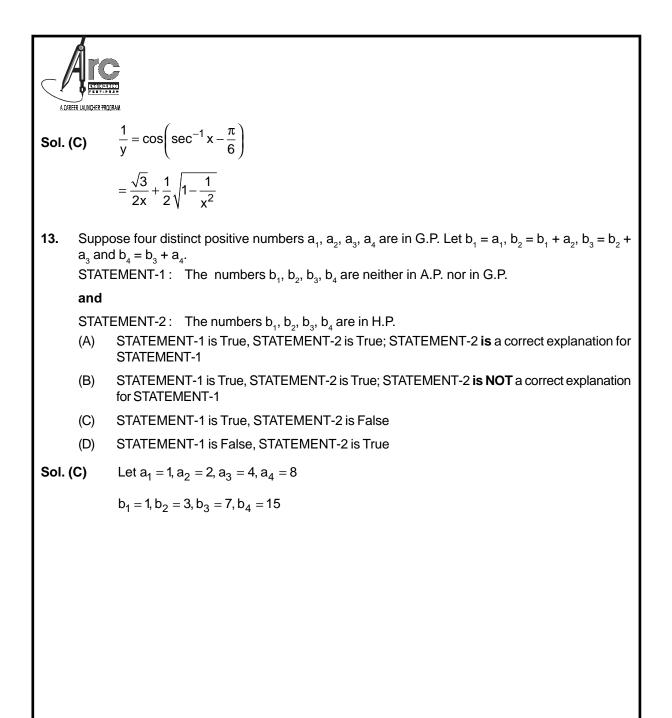
12. Let a solution y = y(x) of the differential equation $x\sqrt{x^2 - 1} dy - y\sqrt{y^2 - 1} dx = 0$ satisfy $y(2) = \frac{2}{\sqrt{3}}$.

STATEMENT-1:
$$y(x) = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$$

and

STATEMENT-2: y(x) is given by $\frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
- (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1
- (C) STATEMENT-1 is True, STATEMENT-2 is False
- (D) STATEMENT-1 is False, STATEMENT-2 is True





SECTION - III

Linked Comprehension Type

This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D) out of which **ONLY ONE** is correct.

Paragraph for Questions Nos.14 to 16.

Consider the lines

$$L_1: \frac{x+1}{3} = \frac{y+2}{1} = \frac{z+1}{2}$$
$$L_2: \frac{x-2}{1} = \frac{y+2}{2} = \frac{z-3}{3}$$

14. The unit vector perpendicular to both
$$L_1$$
 and L_2 is

(A)
$$\frac{-\hat{i}+7\hat{j}+7\hat{k}}{\sqrt{99}}$$
 (B) $\frac{-\hat{i}-7\hat{j}+5\hat{k}}{5\sqrt{3}}$
(C) $\frac{-\hat{i}+7\hat{j}+5\hat{k}}{5\sqrt{3}}$ (D) $\frac{7\hat{i}-7\hat{j}-\hat{k}}{\sqrt{99}}$

Sol. (B)

$$\vec{b}_1 = 3\hat{i} + \hat{j} + 2\hat{k}$$

 $\vec{b}_2 = \hat{i} + 2\hat{j} + 3\hat{k}$
 $\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} i & j & k \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$
 $= \hat{i}(3-4) - \hat{j}(9-2) + \hat{k}(6-1)$
 \therefore Unit vector
 $= \frac{-\hat{i} - 7\hat{j} + 5\hat{k}}{\sqrt{1+49+25}}$
 $\frac{-\hat{i} - 7\hat{j} + 5\hat{k}}{\sqrt{75}}$

15. The shortest distance between L, and L₂ is
(A) 0 (B)
$$\frac{17}{\sqrt{3}}$$

(C) $\frac{41}{5\sqrt{3}}$ (D) $\frac{17}{5\sqrt{3}}$
Sol. (D) $\hat{a}_2 - \hat{a}_1(1+2)\hat{i} + (2-2)\hat{j} + (1+31\hat{x})$
 $= 3\hat{i} + 0\hat{j} + 4\hat{u}$
($a_2 - a_1$) $\cdot (a_1 \times a_2) \begin{vmatrix} 3 & 0 & 4 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix}$
 $3(3-4) + 4(6-1)$
 $-3 + 20 = 17$
S.D = $\frac{17}{\sqrt{75}}$
16. The distance of the point (1, 1, 1) from the plane passing through the point (-1, -2, -1) and whose normal is perpendicular to both the lines L, and L₂ is
(A) $\frac{2}{\sqrt{75}}$ (B) $\frac{7}{\sqrt{75}}$ (C) $\frac{13}{\sqrt{75}}$ (D) $\frac{23}{\sqrt{75}}$
Sol. (C) $a(x+1)+b(y+2)+c(2+1)=0$
 \therefore O Normal of plane is perpendicular to line
 $\Rightarrow \frac{3a+b+2c=0}{a+2b+3c=0}$
 $\frac{a}{3-4} = \frac{b}{2-9} = \frac{c}{6-1}$
 $\frac{a}{3-4} = \frac{b}{2-9} = \frac{c}{6}$
 \therefore Equation of plane is
 $-(x+1)-7(y+2)+5(z+1)=0$
 $-x-1-7y-14+5z+5=0$
 $-x-7y+5z-10=0$

(D) $\frac{23}{\sqrt{75}}$



$$\frac{\left|-1-7+5-10\right|}{\sqrt{1+49+25}} = \frac{13}{\sqrt{75}}$$

Paragraph for Question Nos. 17 to 19

Consider the function $\,f:\left(-\infty,\,\infty\right)\to\left(-\infty,\,\infty\right)$ defined by

$$f(x) = \frac{x^2 - ax + 1}{x^2 + ax + 1}, \, 0 < a < 2$$

Which of the following is true? 17.

(A)
$$(2+a)^2 f''(1) + (2-a)^2 f''(-1) = 0$$

(C) $f'(1)f'(-1) = (2-a)^2$

(B)
$$(2-a)^2 f''(1) - (2+a)^2 f''(-1) = 0$$

(D) $f'(1)f'(-1) = -(2+a)^2$

S

Sol. (A)
$$f(x) = \frac{x^2 - ax + 1}{x^2 + ax + 1}, \ 0 < a < 2$$

$$f'(x) = \frac{(2x - a)(x^2 + ax + 1) - (2x + a)(x^2 - ax + 1)}{(x^2 + ax + 1)^2}$$

$$f'(x) = \frac{2a(x^2 - 1)}{(x^2 + ax + 1)} f'(1) = f'(-1) = 0$$

$$f'(x)(x^2 + ax + 1)^2 - 2a(x^2 - 1) = 0$$

$$f'(x)(x^2 + ax + 1)^2 - 2a(x^2 - 1) = 0$$

$$f''(1)(2 + a)^2 = 4a$$

$$f''(-1)(2 - a)^2 = -4a$$

$$f''(-1)(2 - a)^2 = -4a$$

$$f''(1)(2 + a)^2 + f(-1)(2 - a)^2 = 0$$

$$\therefore (A) \text{ is correct}$$
18. Which of the following is true?
(A) f(x) is decreasing on (-1, 1) and has a local minimum at x = 1
(B) f(x) is increasing on (-1, 1) and has a local maximum nor a local minimum at x = 1
(C) f(x) is increasing on (-1, 1) but has neither a local maximum nor a local minimum at x = 1
(D) f(x) is decreasing on (-1, 1) but has neither a local maximum nor a local minimum at x = 1
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(D) f(x) is decreasing on (-1, 1) but has neither a local maximum nor a local minimum at x = 1
(D) f(x) = \frac{2a(x^2 - 1)}{(x^2 + ax + 1)^2}

A CAREER I ALINCHER F :. $f'(x) < 0, x \in (1,1)$ f'(x) + - + x = 1, Minima hence option (A) is correct Let $g(x) = \int_{0}^{e^{x}} \frac{f'(t)}{1+t^{2}} dt$ 19. Which of the following is true? (A) g'(x) is positive on $(-\infty, 0)$ and negative on $(0, \infty)$ (B) g'(x) is negative on $(-\infty, 0)$ and positive on $(0, \infty)$ (C) g'(x) changes sign on both $(-\infty, 0)$ and $(0, \infty)$ (D) g'(x) does not changes sign on $(-\infty, \infty)$ $g(x) = \int_{0}^{e^{x}} \frac{f'(t)}{1+t^{2}} dt$ Sol. (B) $g'(x) = e^x \cdot \frac{f'(e^x)}{1 + c^{2x}}$ $=e^{x}\cdot\frac{2a(e^{2x}-1)}{1+e^{2x}}$ when x > 0, g'(x) > 0x < 0, g'(x) < 0



Column II

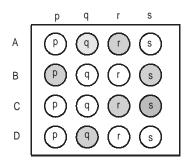
(p) 0

SECTION - IV

Matrix Match Type

The section contains 3 questions. Each question contains statements given in two columns, which have to be matched. Statements in **Column I** are labelled as A, B, C and D whereas statements in **Columns II** are labelled as p, q, r and s. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

If the correct matches are A-q, A-r, B-p, B-s, C-r, C-s and D-q, then the correctly bubbled matrix will look like the following:



20. Match the Statements / Expressions in Column I with the Statements / Expressions in Column II and indicate your answer by darkening the approprite bubbles in the 4 × 4 matrix given in the ORS.

Column II

- (A) The minimum value of $\frac{x^2 + 2x + 4}{x + 2}$ is
- (B) Let A and B be 3 × 3 matrices of real numbers, where A is symmetric, B is key-symmetric, and
 (q) 1

$$(A+B)(A-B) = (A-B)(A+B)$$
. If $(AB)^{t} = (-1)^{k} AB$,

where (AB)^t is the transpose of the matrix AB, then the possible values of k are

(C) Let $a = \log_3 \log_3 2$. An integer k satisfying $1 < 2^{(-k+3^{-a})} < 2^{(-k+3^{-a})}$ (r) 2 must be less than

(D) If
$$\sin \theta = \cos \phi$$
, then the possible value of $\frac{1}{\pi} \left(\theta \pm \phi - \frac{\pi}{2} \right)$ are (s) 3

Sol. $A \rightarrow r, B \rightarrow q, s, C \rightarrow r, s, D \rightarrow p, r$

(A)
$$f(x) = \frac{x^2 + 2x4}{x+2}$$

IIT-JEE 2008 SOLUTIONS PAPER 2

$$f'(x) = 0 \rightarrow x = 0, -4$$

$$x = 0 \text{ is local minima}$$

$$f(0) = 2$$
(B) q,s

$$A' = A, B' = -B, AB = BA$$

$$(AB)^{t} = B^{t}A^{t} = -BA = (-1)^{k}AB$$

$$\Rightarrow (-1)^{K} = -1 \Rightarrow K = 1,3$$
(C) r,s

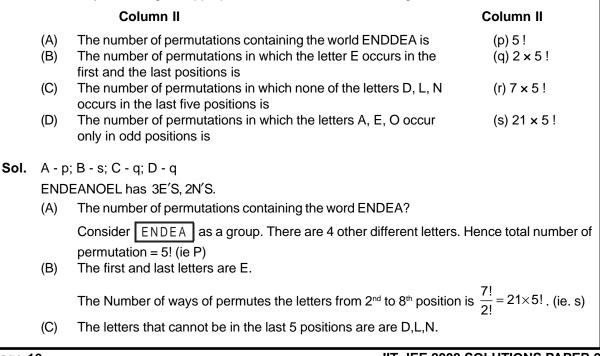
$$2^{0} < 2^{-k+3^{-a}} < 2^{1}$$

$$0 < -k + \log_{2} 3 < 1$$

$$\log_{2} 3 - 1 < k < \log_{2} 3 \Rightarrow k = 1$$
(D) P,

$$r \sin \theta = \cos \phi \Rightarrow \frac{\pi}{2} - \theta = 2n\pi \pm \phi \Rightarrow \frac{1}{\pi} \left(\theta \pm \phi - \frac{\pi}{2} \right) = -2n$$

 Consider all possible permutations of the letters of the word ENDEANOEL Match the Statements / Expressions in Column I with the Statements / Expressions in Column II and indicate your answer by darkening the approprite bubbles in the 4 x 4 matrix given in the ORS.





Hence they have to be arranged in the 1st four position and the rest in the last 5 position. This can be done in

$$\left(\frac{4!}{2!}\right) \times \left(\frac{5!}{3!}\right) = 2 \times 5!$$
 (ie q)

(D) The odd position are 1, 3, 5, 7 and q. A, E, O are only in odd position and the rest in even positions.

This can be done in
$$\left(\frac{5!}{3!}\right) \times \frac{4!}{2!} = 2 \times 5!$$
 (ie q)

22. Consider the lines given by

$$L_1: x + 3y - 5 = 0$$

 $L_2: 3x - ky - 1 = 0$
 $L_3: 5x + 2y - 12 = 0$

Match the Statements / Expressions in **Column I** with the Statements / Expressions in **Column II** and indicate your answer by darkening the approprite bubbles in the 4×4 matrix given in the ORS.

		Column II	Column II
	(A)	L_1, L_2, L_3 are concurrent, if	(p) k = -9
	(B)	One of L_1, L_2, L_3 is parallel to at least one of the other two, if	(q) $k = -\frac{6}{5}$
	(C)	L_1, L_2, L_3 form a triangle, if	(r) $k = \frac{5}{6}$
	(D)	L_1, L_2, L_3 do not form a triangle, if	(s) k = 5
Sol.	$A \to$	$s, B \rightarrow p, q, C \rightarrow r, D \rightarrow p, q, s$	
	L ₁ : x	x + 3y - 5 = 0	
	L ₂ :3	3x - ky - 1 = 0	
	L ₃ : 5	5x + 2y - 12 = 0	
	L ₁ , L ₃	, interest at (2, 1)	
	(A) (S) (B)	For L ₁ , L ₂ , L ₃ to be concurrent $3x - ky - 1 = 0$ must pass through (2, 1). Hence K = 5 (ie s) One of L ₁ , L ₂ , L ₃ to parallel to atleast one of the other two L ₁ , L ₃ are not parallel. So L ₂ has to be either parallel to L ₁ or to L ₃ .	

$$Slope of L_1 = -\frac{1}{3}; L_3 = -\frac{5}{2}$$
Hence Slope of $L_2 = -\frac{1}{3}$ if $\overline{K = -9} \rightarrow P$ or slope of $L_2 = -\frac{5}{2}$ if $\overline{K = -\frac{6}{5}} \rightarrow q$
(C) L_1, L_2, L_3 to form a triangle they must not be concurrent or L2 cannot be parallel to either L_1 or L_3 .
Hence only possibility is $\overline{K = -\frac{6}{5}} \rightarrow r$
(D) L_1, L_2, L_3 cannot form a triangle if $K = 5$ or -9 or $-\frac{6}{5}$ P, q, or S

PHYSICS

PART II

SECTIONS - I

Straight Objective Type

This section contains 9 multiple choice questions. Each questions has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

23. A light beam is traveling from Region I to Region IV (Refer Figure). The refractive index in Regions

I, II, III and IV are $n_0, \frac{n_0}{6}$ and $\frac{n_0}{8}$, respectively. The angle of incidence θ for which the beam just misses entering Region IV is

Figure:

.

Region IRegion IIRegion IIIRegion IV
$$n_0$$
 $\frac{n_0}{2}$ $\frac{n_0}{6}$ $\frac{n_0}{8}$ (A) $\sin^{-1}\left(\frac{3}{4}\right)$ (B) $\sin^{-1}\left(\frac{1}{8}\right)$ (C) $\sin^{-1}\left(\frac{1}{4}\right)$ (D) $\sin^{-1}\left(\frac{1}{3}\right)$

Sol. (B)

If the angle of incidence between Regions III and IV be $\,\phi$, then

$$\frac{n_0}{6}\sin\phi = \frac{n_0}{8}\sin90^\circ$$
$$\Rightarrow \sin\phi = \frac{3}{4}$$

Let the angle of incidence between Regions II and III be $\,\alpha$. Then

$$\frac{n_0}{2}\sin\alpha = \frac{n_0}{6}\sin\phi$$
$$\Rightarrow \sin\alpha = \frac{\sin\phi}{3}$$
But $n_0 \sin\theta = \frac{n_0}{2}\sin\alpha$

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$$\int_{\text{Life Litestitustifies N}} (A) \frac{6\epsilon_0R}{5d+3Vt} = \frac{\sin \theta}{6} = \frac{1}{8}$$

$$(A) \frac{6\epsilon_0R}{5d+3Vt} = \frac{1}{2} = \frac{\sin \theta}{6} = \frac{1}{8}$$

$$(A) \frac{6\epsilon_0R}{5d+3Vt} = \frac{1}{8} =$$



Sol. (A)

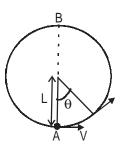
The capacitance is given by

$$C = \frac{t_0}{\left[d - \left(\frac{d}{3} - Vt\right)\right] + \frac{1}{2}\left(\frac{d}{3} - Vt\right)}$$

$$=\frac{6\varepsilon_0}{5d+3Vt}$$

Time constant = RC = $\frac{6\epsilon_0 R}{5d+3Vt}$

26. A bob of mass M is suspended by a massless string of length L. The horizontal velocity V at position A is just sufficient to make it reach the point B. The angle θ at which the speed of the bob is half of that at A, satisfies Figure :



(A)
$$\theta = \frac{\pi}{4}$$
 (B) $\frac{\pi}{4} < \theta < \frac{\pi}{2}$ (C) $\frac{\pi}{2} < \theta < \frac{3\pi}{4}$ (D) $\frac{3\pi}{4} < \theta < \pi$

Sol. (D)

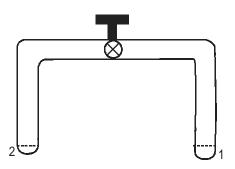
 $V = \sqrt{5gL}$

Since mechanical energy is conserved,

$$\frac{1}{2}m(5gL) = \frac{1}{2}m\left(\frac{5gL}{4}\right) + mgh$$
$$\Rightarrow h = \frac{15L}{8} = L + \frac{7L}{8}$$
$$\Rightarrow L(1 - \cos\theta) = L\left(1 + \frac{7}{8}\right)$$
Clearly, $-1 < \cos\theta < -\frac{1}{\sqrt{2}} \qquad \Rightarrow \frac{3\pi}{4} < \theta < \pi$



27. A glass tube of uniform internal radius (r) has a valve separating the two identical ends. Initially, the valve is in a tightly closed position. End 1 has a hemispherical soap bubble of radius r. End 2 has sub-hemispherical soap bubble as shown in figure. Just after opening the valve, Figure :



(A) air from end 1 flows towards end 2. No change in the volume of the soap bubbles

(B) air from end 1 flows towards end 2. Volume of the soap bubble at end 1 decreases (C) no change occurs

(D) air from end 2 flows towards end 1. Volume of hte soap bubble at end 1 increases **Sol. (B)**

Let the radius of the bubble at end 2 be R. Then R > r.

Now,
$$P_2 - P_0 = \frac{4T}{R}$$

 $\Rightarrow P_2 = P_0 + \frac{4T}{R}$
And, $P_1 - P_0 = \frac{4T}{r}$
 $\Rightarrow P_1 = P_0 + \frac{4T}{r}$
 $\therefore P_1 > P_2$
 \Rightarrow Air will flow from P_1

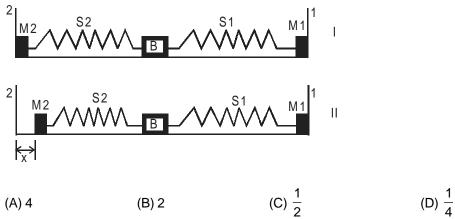
 \Rightarrow Air will flow from end 1 to 2, and as a result volume at end 1 decreases.



28. A block (B) attached to two unstretched springs S1 and S2 with spring constants k and 4k, respectively (see figure 1). The other ends are attached to identical supports M1 and M2 not attached to hte walls. The springs and supports have negligible mass. There is no friction anywhere. The block B is displaced towards wall 1 by a small distance x (figure II) and released. The block returns and moves a maximum distance y towards wall 2. Displacements x and y are measured

with respect to hte equilibrium position of the block B. The ratio $\frac{y}{y}$ is

Figure :



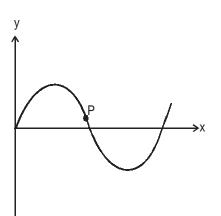
Sol. (C)

Energy of the system (B + springs) will be conserved.

$$\therefore \frac{1}{2}Kx^2 = \frac{1}{2}(4K)y^2$$
$$x = 2y$$
$$\therefore \frac{y}{x} = \frac{1}{2}$$



29. A transverse sinusoidal wave moves along a string in the positive x-direction at a speed of 10 cm/ s. The wavelength of the wave is 0.5 m and its amplitude is 10 cm. At a particular time t, the snapshot of the wave is shown in figure. The velocity of point P when its displacement is 5 cm is Figure :



(A)
$$\frac{\sqrt{3}\pi}{50}\hat{j}$$
 m/s (B) $-\frac{\sqrt{3}\pi}{50}\hat{j}$ m/s (C) $\frac{\sqrt{3}\pi}{50}\hat{i}$ m/s (D) $-\frac{\sqrt{3}\pi}{50}\hat{i}$ m/s

Sol. (A)

$$K = \frac{2\pi}{\lambda} = 4\pi \text{ rad/m}$$

 $\omega = Kv = 4\pi.0.1 = 0.4\pi \text{ rad/s}$

 $\therefore y = 0.1 \sin(4\pi x - 0.4\pi t)$

Suppose the snapshot shown is at t = 0.

 \therefore y = 0.1sin(4 π x)

For P,

 $0.05 = 0.1 \sin(4\pi x)$

 $\therefore \sin 4\pi x = 0.5$ Now velocity of P:

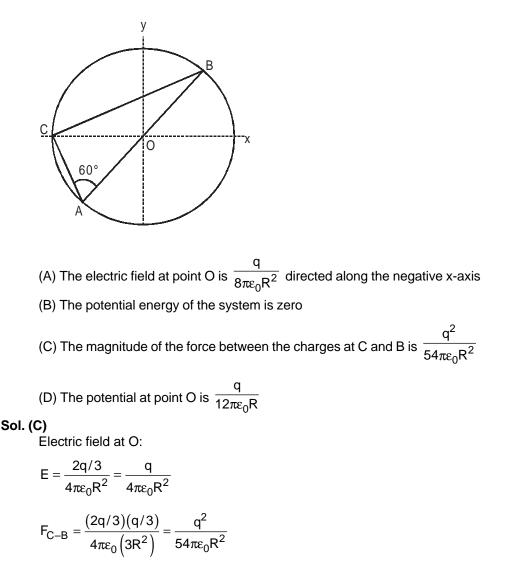
$$v = \frac{dy}{dt} = -0.04\pi \cos(4\pi x - 0.4\pi t)$$

At t = 0,
$$v = -0.04\pi \cos 4\pi x$$
$$= -0.04\pi \left(\pm\sqrt{(1 - 0.25)}\right) = \frac{\pi\sqrt{3}}{50} \quad \left(\because x > \frac{\pi}{2}\right)$$

s



30. Consider a system of three charges $\frac{q}{3}, \frac{q}{3}$ and $-\frac{2q}{3}$ placed at points A, B and C, respectively, as shown in the figure. Take O to be the centre of the circle of radius R and angle CAB = 60° Figure :





- **31.** A radioactive sample S1 having an activity of 5μCi has twice the number of nuclei as another sample S2 which has an activity of 10μCi. The half lives of S1 and S2 can be
 - (A) 20 years and 5 years, respectively

(B) 20 years and 10 years, respectively

(C) 10 years each

(D) 5 years each

Sol. (A)

 $5\mu Ci = \lambda(2N)$

and $10\mu Ci = \lambda(N)$

$$\Rightarrow \frac{\lambda_1}{\lambda_2} = \frac{5}{20} = \frac{1}{4}$$
$$\Rightarrow \frac{T_1}{T_2} = \frac{4}{1}$$

SECTION – II

Reasoning Type

This section contains 4 reasoning type questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct

32. STATEMENT -1

It is easier to pull a heavy object than to push it on a level ground.

and

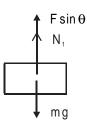
STATEMENT -1

The magnitude of frictional force depends on the nature of the surfaces in contact.

- (A) STATEMENT -1 is True, STATEMENT -2 is True; STATEMENT -2 is a correct explanation for STATEMENT -1
- (B) STATEMENT -1 is Trure, STATEMENT -2 is True; STATEMENT -2 is NOT a correct explanation for STATEMENT -1
- (C) STATEMENT -1 is True, STATEMENT -2 is False
- (D) STATEMENT -1 is False, STATEMENT -2 is True
- Sol.

In pulling case

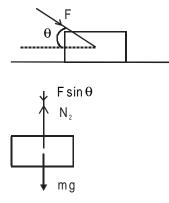




 \therefore N + F sin θ = mg

 $N_1 = (mg - F\sin\theta)$

In Pushing case



 $N_2 = (F \sin \theta + mg)$

Normal force $\rm N_{2}$ in pushing is more than the normal force $\rm N_{1}$ in pulling.

 $\therefore f = \mu N$

so if is easier to pull a heavy object than to push

so, statement - I is right & and of friction force also repel on surface of nature.

Therefore statement (I) & statement (II) both are right & statement (II) is not the correct explanation of statement (I)

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33. STATEMENT-1				
55.				
	For practical purposes, the earth is used as a reference at zero potential in electrical circuits.			
	and			
	STATEMENT-2			
	The electrical potential of a sphere of radius R with charges Q uniformly distributed on the surface			
	0			
	is given by $\frac{Q}{4\pi\epsilon_0 R}$.			
	$4\pi\epsilon_0 R$			
	(A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for			
	STATEMENT-1			
	(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation			
	for STATEMENT-1			
	(C) STATEMENT-1 is True, STATEMENT-2 is False			
	(D) STATEMENT-1 is False, STATEMENT-2 is True			
Sol.				
001.	Both the statements are true & statement (II) is not the correct explanation of statement (I)			
	Both the statements are true, & statement (II) is not the correct explanation of statement (I).			
	Because, whatever be the value of potential we can assign it zero as a reference.			
34.	STATEMENT-1			
	The sensitivity of a moving-coil galvanometer is increased by placing a suitable magnetic material			
	as a core inside the coil.			
	and			
	STATEMENT-2			
	Soft iron has a high magnetic permeability and cannot be easily mangetized or demagnetized.			
	(A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for			
	STATEMENT-1			
	(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation			
	for STATEMENT-1			
	(C) STATEMENT-1 is True, STATEMENT-2 is False			
	(D) STATEMENT-1 is False, STATEMENT-2 is True			
Sol.				
	(range of output)			
	Sensitivity = $\left(\frac{\text{range of output}}{\text{range of Input}}\right)$			
	By placing suitable magnetic material as a were inside the coil, the magnetic moment of the coil			
	will increase so, torque $\vec{\tau}$ which is equal to MB sin θ will increase.			
	That's why we will find more range of output for a given range of input in a galvanometer.			
	.: Statement (I) is correct			
	Highly permeable magnetic material easily magnetized & easily demagnetise.			
	Statement (II) is wrong.			

 \therefore Statement (II) is wrong.



35. STATEMENT-1

For an observer looking out through the window of a fast moving train, the nearby objects appear to move in the opposite direction to the train, while the distant objects appear to be stationary. and

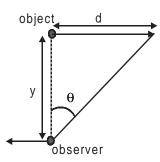
STATEMENT-2

If the observer and the object are moving at velocities $\overline{V_1}$ and $\overline{V_2}$ respectively with reference to a

laboratory frame, the velocity of the object with respect to the observer is $\overrightarrow{V_2} - \overrightarrow{V_1}$.

- (A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1
- (B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is NOT a correct explanation for STATEMENT-1
- (C) STATEMENT-1 is True, STATEMENT-2 is False
- (D) STATEMENT-1 is False, STATEMENT-2 is True





y = Distance in between observer & object d = relative displacement between observer & object

$$\tan \theta = \left[\frac{d}{y}\right]$$

If y is very large, then angle subtended by displacement d in a given time is very small as compare to nearer object.

so statement (I) is correct.

Now, observer velocity w,r.t laboratory frame = V_1 & object " " " = V_2

: Velocity of the object w.r.t observer $\vec{V}_{21} = \vec{V}_2 - \vec{V}_1$

so statement (II) is also correct.



SECTION -III

Linked Comprehension Type

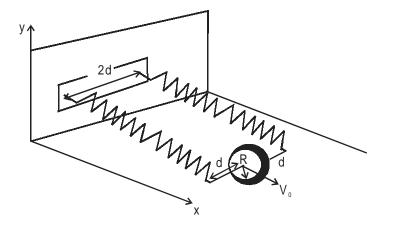
This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

Paragraph for Questions Nos. 36 to 38

A uniform thin cylindrical disk of mass M and radius R is attached to two id enthical massless springs of spring constant k which are fixed to the wall as shown in the figure. The springs are attached to hte axle of hte disk symmetrically on either side at a distance d from its centre. The axle is massless and both the springs and the axle are in a horizontal plane. The unstretched length of each spring is L. The disk is initially at its equilibrium position with its centre of mass (CM) at a distance L from the wall. The

disk rolls without slipping with velocity $\overline{V_0} = V_0 \hat{i}$. The coefficient of friction is μ .

Figure :



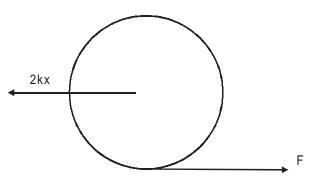
36. The net external force acting on the disk when its centre of mass is at displacement x with respect to its equilibrium position is



Sol.



for translational motion



2kx – F = Ma(1) for rotational motion

$$FR = I\alpha = \frac{MR^2}{2} \left(\frac{a}{R}\right)....(2)$$

from (1) and (2) $F = \frac{ma}{2}$

$$a = -\frac{4kx}{3m}$$

Force = Ma =
$$-\frac{4kx}{3m}$$
 (D)

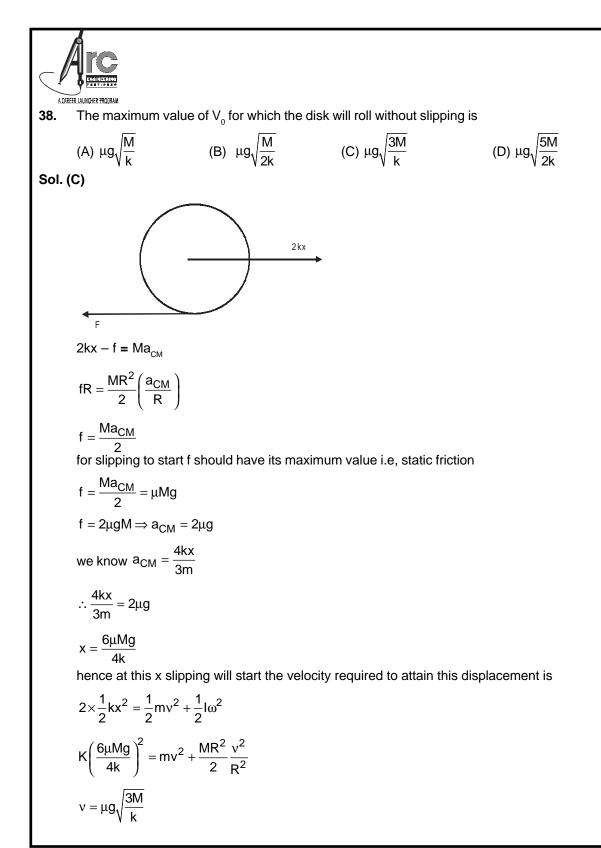
37. The centre of mass of the disk undergoes simple harmonic motion with angular frequency ω equal to

(A)
$$\sqrt{\frac{k}{M}}$$
 (B) $\sqrt{\frac{2k}{M}}$ (C) $\sqrt{\frac{2k}{3M}}$ (D) $\sqrt{\frac{4k}{3M}}$

Sol. (D)

From the above question it is evident that net restoring force

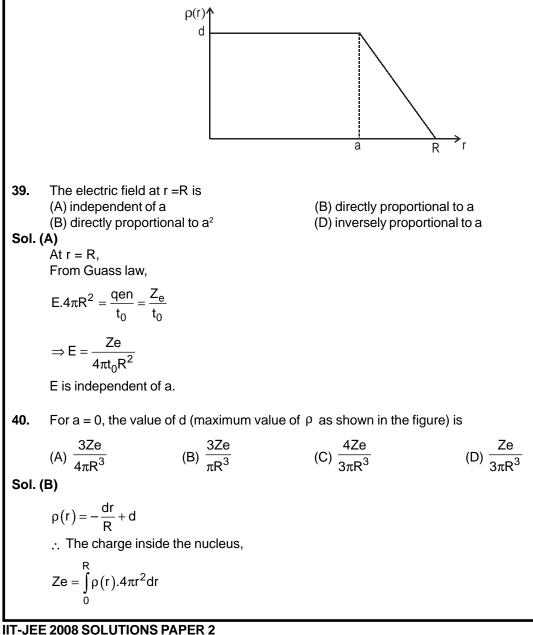
$$F = -\frac{4kx}{3M}$$
$$\therefore \omega = \sqrt{\frac{4k}{M}}$$





Paragraph for Question Nos. 39 to 41

The nuclear charges (Ze) is non-uniformly distributed within a nucleus of radius R. The charge density $\rho(r)$ [charge per unit volume] is dependent only on the radial distance r form the centre of the nucleus as shown in figure. The electric field is only along the radial direction. Figure :



$$interms = \frac{R}{2} \left\{ \left(-\frac{d}{R} \cdot r + d \right) 4\pi r^2 \right\}$$
$$= 4\pi \left[-\frac{d}{R} \cdot \frac{r^4}{4} + d \cdot \frac{r^3}{3} \right]_0^R$$
$$= 4\pi d \left[-\frac{R^3}{4} + \frac{R^3}{3} \right]$$
$$or, Ze = \frac{\pi d R^3}{3}$$
$$\Rightarrow d = \frac{3Ze}{\pi R^3}$$

}dr

41. The electric field within the nucleus is generally observed to be linearly dependent on r. This implies

(A)
$$a = 0$$
 (B) $a = \frac{R}{2}$ (C) $a = R$ (D) $a = \frac{2R}{3}$

Sol. (C)

Electric field within the nucleus is linearly dependent on r is possible when the charge distribution is uniform.

∴ a = R

$$E.4\pi r^{2} = \frac{qen}{t_{0}} = \frac{d.\frac{4}{3}\pi r^{2}}{t_{0}}$$
$$\Rightarrow E = \left(\frac{1}{3t_{0}}d\right)r$$
$$E \propto r$$

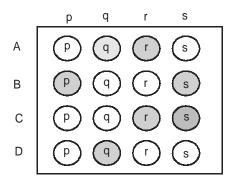


SECTION - IV

Matrix Match Type

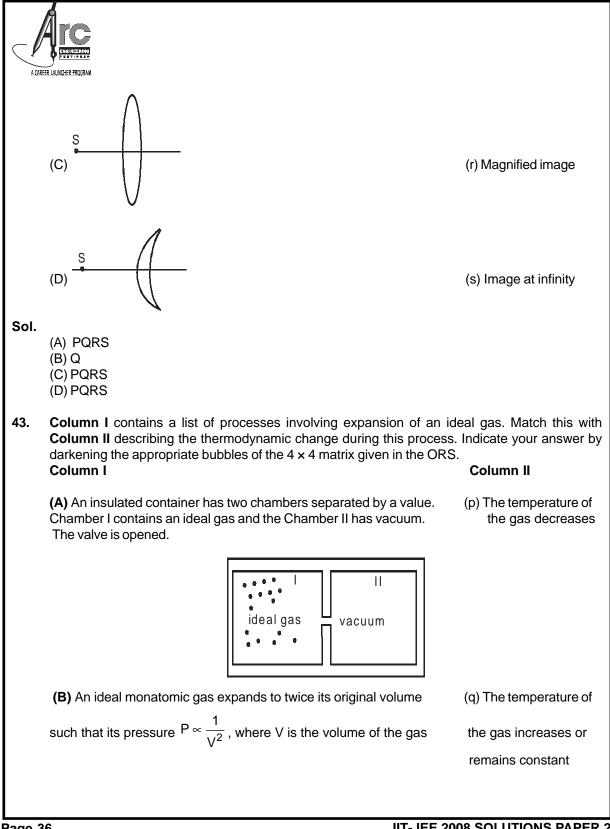
The section contains 3 questions. Each question contains statements given in two columns, which have to be matched. Statements in **Column I** are labelled as A, B, C and D whereas statements in **Columns II** are labelled as p, q, r and s. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

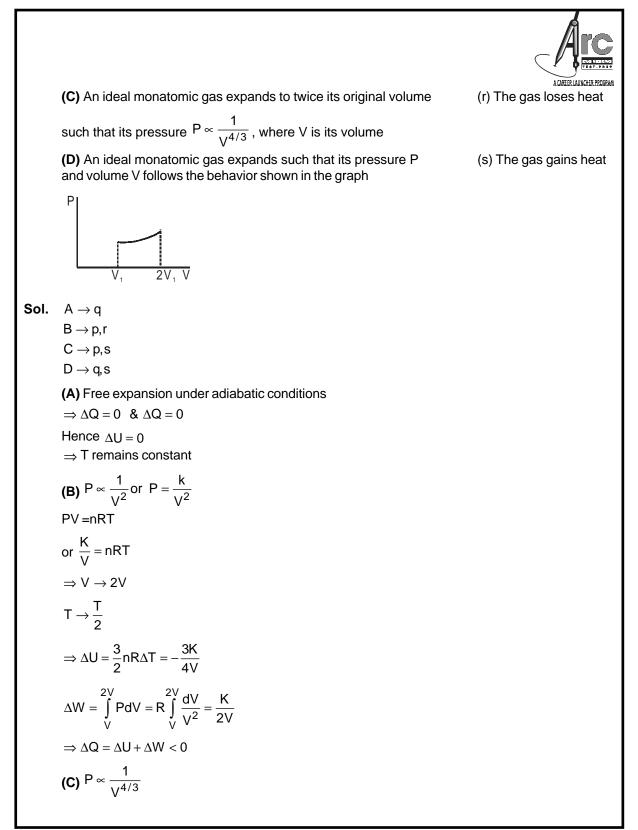
If the correct matches are A-q, A-r, B-p, B-s, C-r, C-s and D-q, then the correctly bubbled matrix will look like the following:

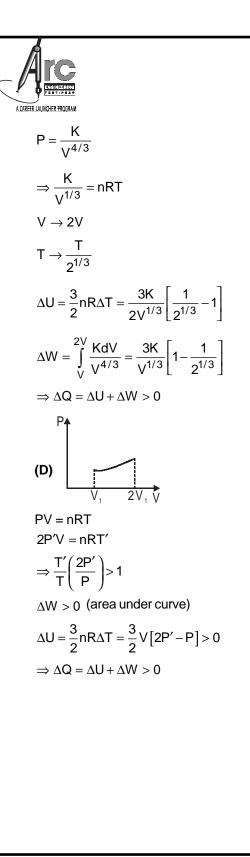


42. An optical component and an object S placed along its optic axis are given in Column I. The distance between the object and the component can be varied. The properties of images are given in Column II. Match all the properties of images from Column II. Match all the properties of images from Column II. Indicate your answer by darkening the appropriate bubbles of the 4 x 4 matrix given in the ORS. Column I





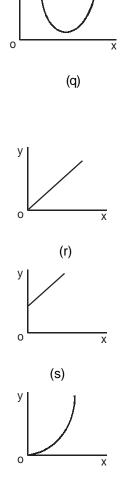




44. Column I give a list of possible set of parameters measured in some experiments. The variations of the parameters in the form of graphs are shown in Column II. Match the set of parameters given in Column I with the graph given in Column II. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix given in the ORS. Column I Column II

(A) Potential energy of a simple pendulum (y axis) as a function of displacement (x axis)

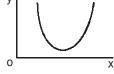
- (B) Displacement (y axis) as a function of time (x axis) for a one dimensional motion at zero or constant acceleration when the body is moving along the positive x-direction
- (C) Range of a projectile (y axis) as a function of its velocity (x axis) when projected at a fixed angle
- (D) The square of the time period (y axis) of a simple pendulum as a function of its length (x axis)

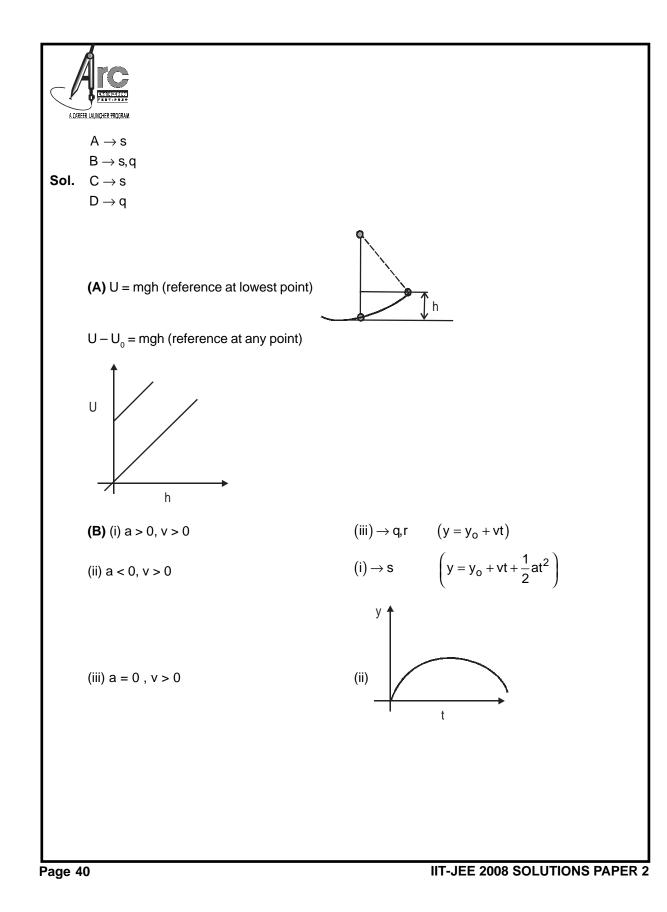




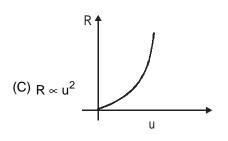


(p)

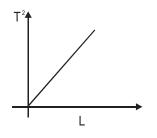














CHEMISTRY

PART III

Section – I

Straight Objective Type

This section contains 9 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D), out of which only one is correct.

45. Solubility product constants (K_{sp}) of salts of types MX, MX₂ and M₃X at temperature "T" are

 4.0×10^{-8} , 3.2×10^{-14} and 2.7×10^{-15} , respectively. Solubilities (mol dm⁻³) of the salts at temperature "T" are in the order

(A) $MX > MX_2 > M_3X$ (B) $M_3X > MX_2 > MX$ (C) $MX_2 > M_3X > MX$ (D) $MX > M_3X > MX_2$

Sol. (D)

Solubility of MX = 0.0002 moles/dm³ Solubility of MX₂ = 0.00002 moles/dm³ Solubility of M₃X = 0.0001

46. Electrolysis of dilute aqueous NaCl solution was carried out by passing 10 milli ampere current. The time required to liberate 0.01 mol of H_2 gas at the cathode is (1 Faraday = 96,500 C mol⁻¹)

(A) 9.6×10^4 sec (B) 19.3×10^4 sec (C) 28.95×10^4 sec (D) 38.6×10^4 sec Sol. (B)

 $w = zIt \text{ or } n \rightarrow number \text{ of moles} = \frac{it}{96500 \text{ } n \rightarrow n - factor}$

- $0.01 = \frac{10 \times 10^{-3} \times t}{96,500 \times 2}$ t = 19.3×10⁴ sec.
- **47.** Among the following, the surfactant that will form micelles in aqueous solution at the lowest molar concentration at ambient conditions is

(A)
$$CH_3(CH_2)_{15}N^+(CH_3)_3Br^-$$

(B) $CH_3(CH_2)_{11}OSO_3^-Na^+$

(C) $CH_3(CH_2)_6COO^-Na^+$

(D) $CH_3(CH_2)_{11}Na^+(CH_3)_3Br^-$

Sol. (B)



- Both $\left[Ni(CO)_{4}\right]$ and $\left[Ni(CN)_{4}\right]^{2-}$ are diamagnetic. The hybridisations of nickel in these 48. complexes, respectively are
 - (A) sp^3 , sp^3 (B) sp^3 , dsp^2 (C) dsp^2 , sp^3 (D) dsp^2 , dsp^2

Sol. (B)

 $Ni(CO)_4 \longrightarrow sp^3$ $\left[\operatorname{Ni}(\operatorname{CN})_{4}\right]^{2} \longrightarrow \operatorname{dsp}^{2}$

The IUPAC name of $\left[Ni(NH_3)_4 \right] [NiCl_4]$ is 49.

- (A) Tetrachloronickel (II) tetraamminenickel (II)
- (B) Tetraamminenickel (II) tetrachloronickel (II)
- (C) Tetraamminenickel (II) tetrachloronickelate (II)
- (D) Tetrachloronickel (II) tetraamminenickelate (0)

Sol. (C)

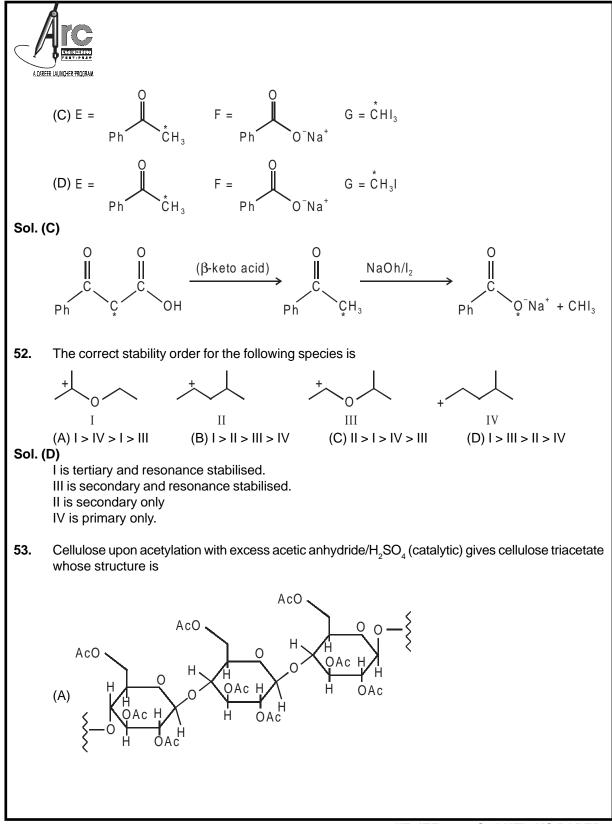
Tetrammine nickel (II) - tetrachloro nickelate (II)

50. Among the following, the coloured compound is

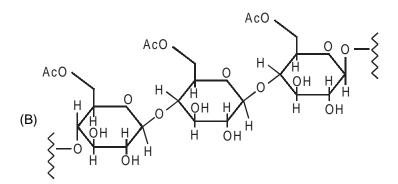
(B) $K_3 \left[Cu(CN)_4 \right]$ (A) CuCl (D) $\left[Cu(CH_3CN)_4 \right] BF_4$ (C) CuF₂ **Sol. (C)** CuF₂

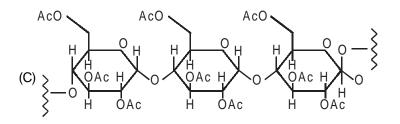
In the following reaction sequence, the correct structures of E, F and G are 51.

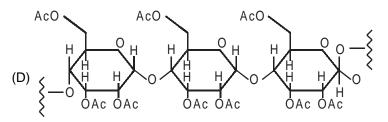
$$(A) E = Ph \xrightarrow{Heat} (B) E = Ph \xrightarrow{Heat} (CH_3) F = Ph \xrightarrow{O} (CH_3) F = Ph \xrightarrow{O} (O^-Na^+) G = CHI_3$$











Sol. (A)

Cellulose is made up from β -D glucose.

Section II

This section contains 4 reasoning type questions. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

54. STATEMENT-1:
$$[Fe(H_2O)_5 NO]SO_4$$
 is paramagnetic.

and

STATEMENT-2: The Fe in $\left[Fe(H_2O)_5 NO\right]SO_4$ has three unpaired electrons.

(A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1



A CAREER LAUNCHER PROGRAM

(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1

(C) STATEMENT-1 is True, STATEMENT-2 is False

(D) STATEMENT-1 is False, STATEMENT-2 is True.

Sol. (A)

Oxidation state of Fe is +1, charges on NO is +1 and Fe⁺ has three unpaired electrons.

55. STATEMENT-1: The geometrical isomers of the complex $\left[M(NH_3)_4 Cl_2\right]$ are optically inactive.

and

STATEMENT-2: Both geometrical isomers of the complex $\left[M(NH_3)_4 Cl_2\right]$ possess axis of

symmetry.

(Å) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1

(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1

(C) STATEMENT-1 is True, STATEMENT-2 is False

(D) STATEMENT-1 is False, STATEMENT-2 is True.

Sol. (A)

56. STATEMENT-1: There is a natural asymmetry between converting work to heat and converting heat to work

and

STATEMENT-2: No process is possible in which the sole result is the absorption of heat from a reservoir and its complete conversion into work.

(A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1

(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1

(C) STATEMENT-1 is True, STATEMENT-2 is False

(D) STATEMENT-1 is False, STATEMENT-2 is True.

Sol. (A)

57. STATEMENT-1 : Aniline on reaction with NaNO₂/HCl at 0 °C followed by coupling with β -naphthol gives a dark blue coloured precipitate.

and

STATEMENT-2 : The colour of the compound formed in the reaction of aniline with NaNO₂/HCl at 0 °C followed by coupling with β -naphthol is due to the extended conjugation.

(A) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is a correct explanation for STATEMENT-1

(B) STATEMENT-1 is True, STATEMENT-2 is True; STATEMENT-2 is **NOT** a correct explanation for STATEMENT-1

(C) STATEMENT-1 is True, STATEMENT-2 is False

(D) STATEMENT-1 is False, STATEMENT-2 is True.

Sol. (D)



SECTION - III

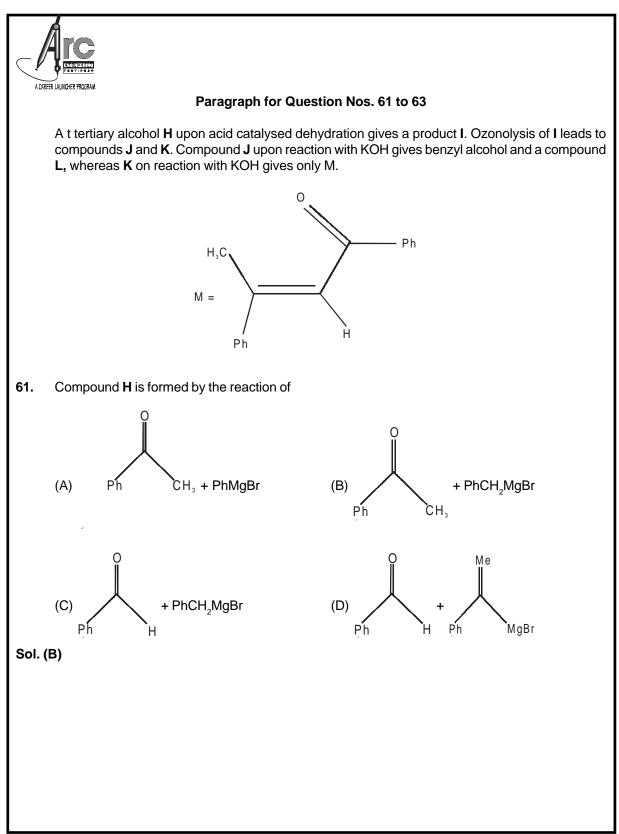
Linked Comprehension Type

This section contains 2 paragraphs. Based upon each paragraph, 3 multiple choice questions have to be answered. Each question has 4 choices (A), (B), (C) and (D), out of which **ONLY ONE** is correct.

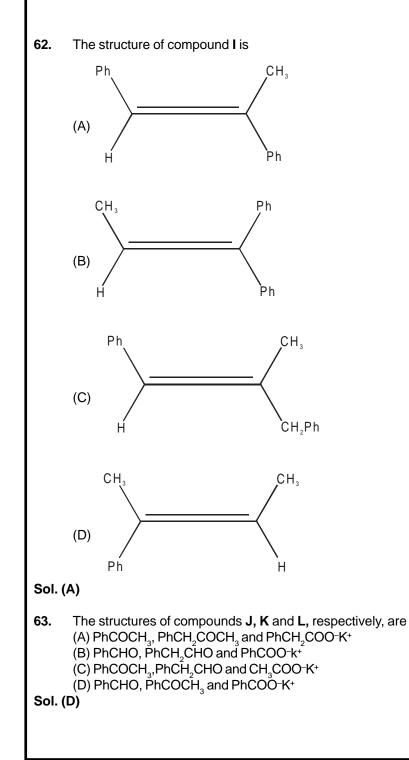
Paragraph for Question Nos. 58 to 60

In hexagonal systems of crystals, a frequently encountered arrangement of atoms is described as a hexagonal prism. Here, the top and bottom of the cell are regular hexagonas and three atoms are sandwiched in between them. A space-fillingt model of this structure, called hexagonal close-packed (HCP), is contituted of a sphere on a flat surface surrounded in the same plane by six identical spheres as closely as possible. Three spheres are then placed over the first layer so that they touch each other and represent the second layer. Each one of these three spheres touches three spheres of the bottom layer. Finally, the second layer is covered with a third layer that is identical to the bottom layer in relative position. Assume radius of every sphere to be 'r'.

58.	The number of atoms (A) 4	in this HCP unit cell is (B) 6	(C) 12	(D) 17		
Sol. ((B) 6					
59.	The volume of this CHP unit cell is					
	(A) $_{24\sqrt{2}r}^{3}$	(B) $16\sqrt{2}r^3$	(C) $12\sqrt{2}r^3$	(D) $\frac{64}{3\sqrt{3}}r^3$		
Sol. (A)						
	$24\sqrt{2}r^3$					
60.	The empty space in th (A) 74%	is HCP unit cells is (B) 47.6%	(C) 32%	(D) 26%		
Sol. (D) Packing fraction is HCP unit cell is 74% \therefore the emptyspace is 100 – 74 = 26%						
	J. J					

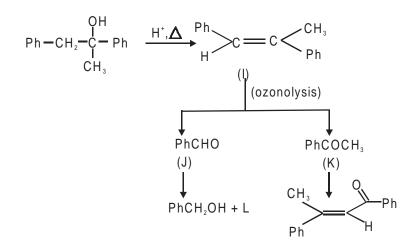








Explanation for questions 61 to 63





SECTION - IV

Maxtrix Match Type

This section contains 3 questions. Each question contains statements given in two columns, which have to be matched. Statements in **Column I** are labelled as A, B, C and D whereas statements in **Column II** are labelled as p, q, r and s. The answers to these questions have to be appropriately bubbled as illustrated in the following example.

If the correct matches are A-q, A-r, B-p, B-s, C-r, C-s and D-q, then the correctly bubbled matrix will look like the following.

64. Match the conversions in Column I with the type(s) of reaction(s) given in Column II. Indicate your answer by darkening the appropriate bubbles of the 4 × 4 matrix given in the ORS Column I

(A) $PbS \rightarrow PbO$	(p) roasting
(B) $CaCO_3 \rightarrow CaO$	(q) Calcination
(C) $ZnS \rightarrow Zn$	(r) carbon reduction
(D) $Cu_2S \rightarrow Cu$	(s) self reduction

Sol.

- A p B - q
- C p, r
- D p, s

65. Match the entries in Column I with the correctly related quantum number(s) in Column II. Indicate your answer by darkening the appropriate bubbles of the 4 × 4 matrix given in the ORS Column I Column II

- (A) Orbital angular momentum of the electronin a hydrogen-like atomic orbitalb
- (B) A hydrogen-like one-electron wave function obeying Pauli principle
- (C) Shape, size and orientation of hydrogen -like atomic orbitals
- (D) Probability density of electron at the nucleus in hydrogen-like atom

Sol.

- A q
 - B s
 - C p, q, r
 - D p, q, r

(q) Azimuthal quantum number

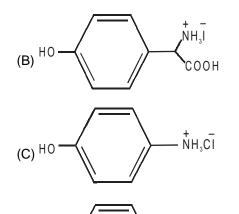
(p) Principal quantum number

- (r) Magnetic quantum number
- (s) Electron spin quantum number



66. Match the compounds in Column I with their characteristic test(s)/reactions(s) given in Column II. Indicate your answer by darkening the appropriate bubbles of the 4 × 4 matrix given in the ORS. Column I

(A)	$H_2N - \overset{\oplus}{N}H_3$	e CI
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NH-NH₃Br

NO,

(p) sodium fusion extract of the compound give Prussian blue colour with FeSO₄

(q) gives positive FeCl₃ test

(r) gives white precipitate with AgNO₃

(s) reacts with aldehydes to form the

corresponding hydrazone derivative

Sol.

A - r, s B - q, p C - r, q, p D - p, s

02N

(D)